



**80** Pages  
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# EXERCISE BOOK CAHIER D'EXERCICES

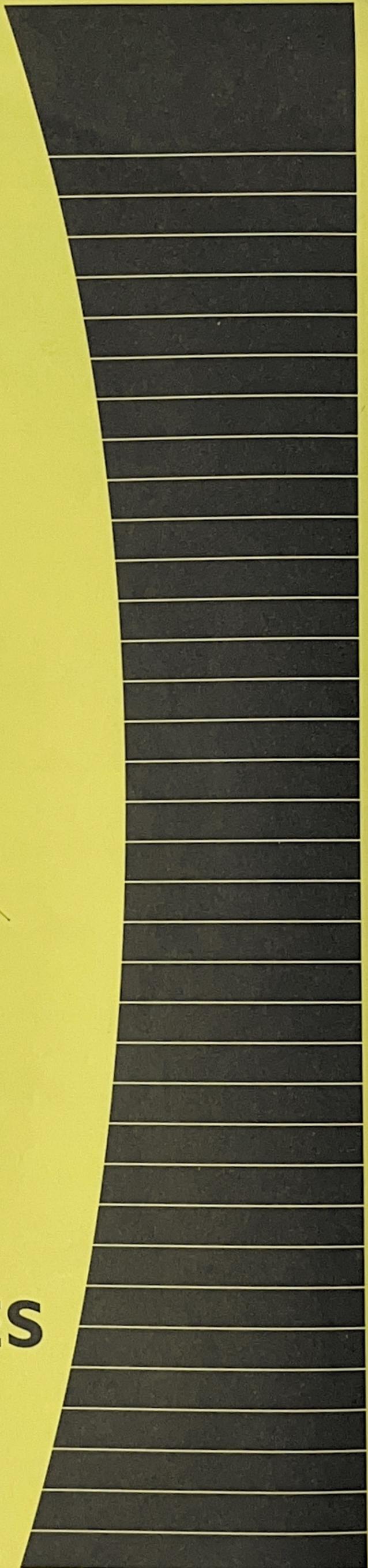
NAME/NOM Cole Shanks

SUBJECT/SUJET ELEC 301



ASSEMBLED IN CANADA WITH IMPORTED MATERIALS  
ASSEMBLÉ AU CANADA AVEC DES MATIÈRES IMPORTÉES

12107



# Lecture 0

9/05/19

LEC

## Course Overview:

Mini Projects (15% each)  $\rightarrow$  60%

BiWeekly tests (10% each)  $\rightarrow$  40%

Office Hour  $\rightarrow$  KATS 3040 or 3041

Mini Project 2 DIFFICULT

$\rightarrow$  3 weeks extended, so

also for test then

Email Subject: ELEC301F19 followed by a space and question/subject.

9/09/19

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## Lecture 1

Figure 3  $\rightarrow$  Figure 4 (Miller's Thrm)

9/10/19

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## Lecture 2

9/12/19

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## Lecture 3

$20 \log(\sqrt{2}) = 3\text{dB}$  \*0.707 used often as a point

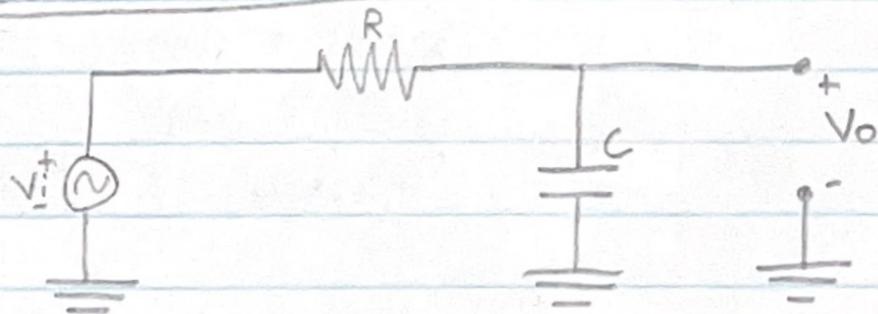
9/16/19

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## Lecture 4

\*Review Bode plots (Phase and amplitude)

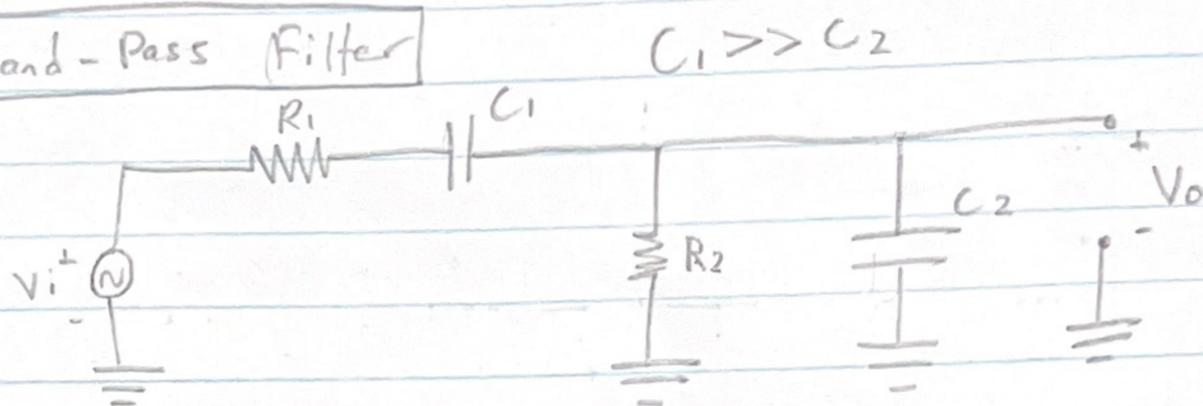
### Low-Pass Filter



### Questions:

- ① Capacitor @ high  $\omega \rightarrow$  short
- @ low  $\omega \rightarrow$  open
- How does  $C$  values influence this behaviour?

### Band-Pass Filter



### Large Blocking Capacitor:

Because  $C_1 \gg C_2$

$\rightarrow$  terms like  $\left( \frac{1}{R_2 C_2} + \frac{1}{R_1 C_1} \right) \rightarrow \frac{1}{R_2 C_2}$

9/17/19  
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## Lecture 5

3dB (half power point):

**P7.4** \* Understand this slide

Find Cutoff Frequencies: (High and Low)

- ① Poles are known
- ② Have circuit but don't know poles

**P7.10**

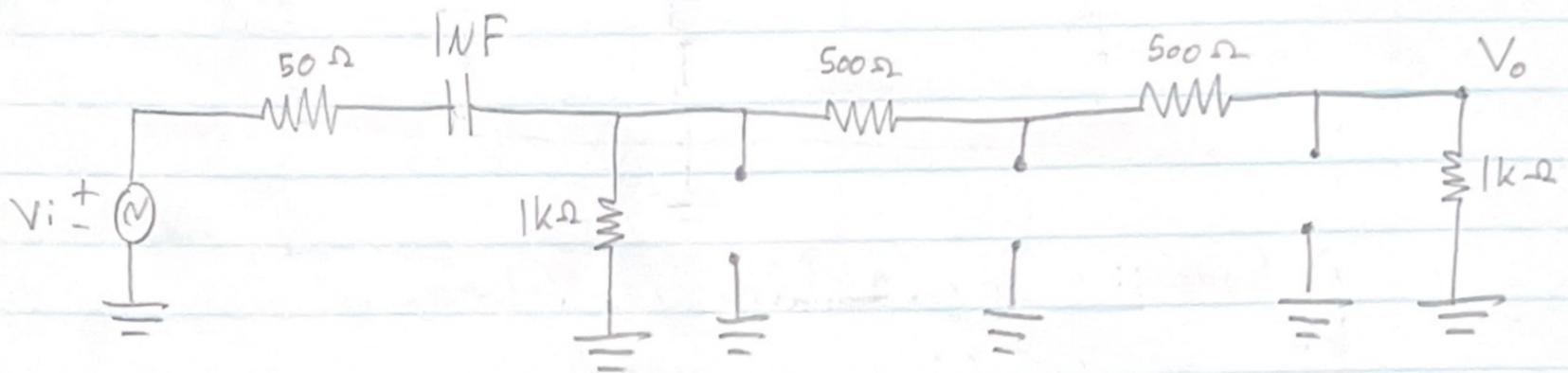
Short circuit time constants:

• short all other capacitors and  $V$  sources and get resistance ( $a \rightarrow b$  therein) across the capacitor you're looking at

# Lecture 6

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## Problem set 2 Q3:



$$(1E-6)(50 + 1k || 2k)$$

$$= 0.000716 = \tau_{oc}$$

$$\frac{1}{0.000716} = 1395.35 \rightarrow \omega_{L3dB} = 1395.35/s$$

Time constants:

$$\omega_p = \frac{1}{\tau_{oc}}$$

\*Important  $\rightarrow$  P 7.4 (30B)

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# Lecture 7

## Problem Set 2:

Q1

$$\tau_{c1}^{oc} = C_1(R_1 + R_2) \quad [\text{short source, open } C_2]$$

$$\tau_{c2}^{oc} = C_2 R_2 \quad [\text{short source, open } C_1]$$

\*  $d_1 =$  Sum of the open circuit time constants

Q4

$$\omega_{z1L} = 100/s \quad \omega_{L3dB} = \sqrt{(200/s)^2 + (50/s)^2 - 2 \cdot (100/s)^2}$$

$$\omega_{z2L} = 0/s \quad = 150/s$$

$$\omega_{p1L} = 200/s$$

$$\omega_{p2L} = 50/s$$

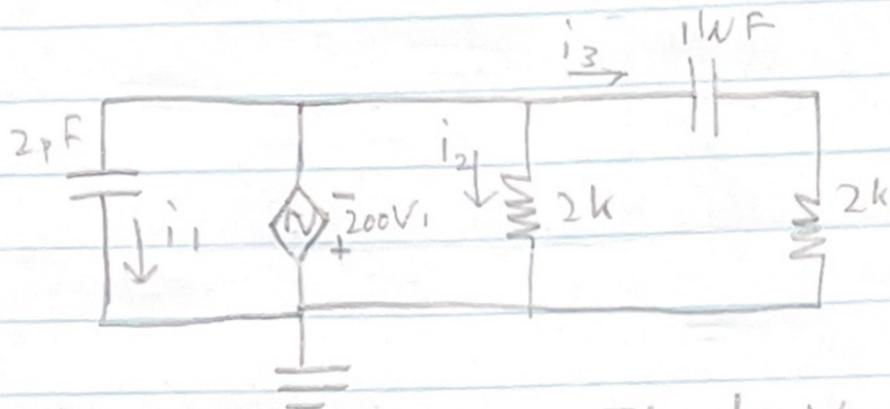
What is  $\omega_{L3dB} = ?$

# Lecture 9

9/26/19

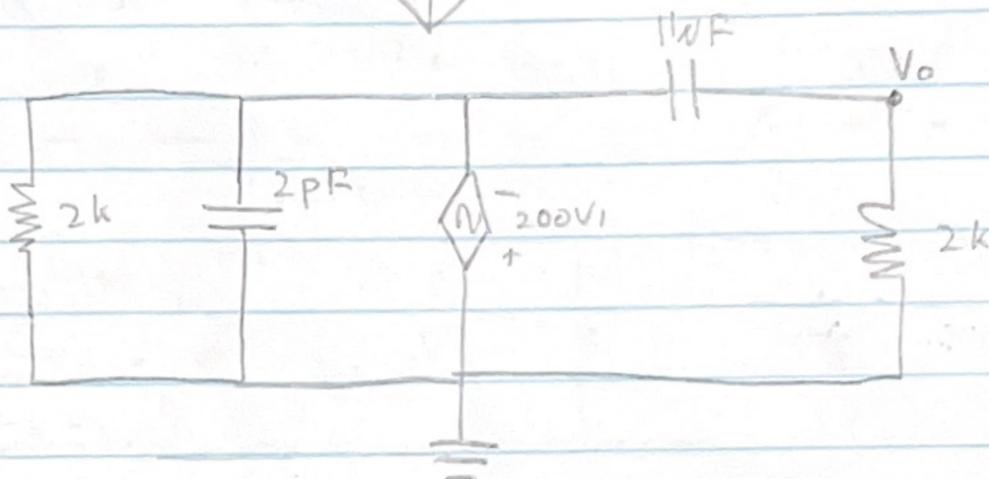
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PS2 Q5



Ideal  $V_{source}$

[really 3 parallel circuits]



$$V_0 = i_3 \cdot 2k$$

~~$$-200V_1 = i_3 \cdot 2k$$~~

$$-200V_1 = i_3 \left( \frac{1}{j\omega \cdot 1\mu F} + 2k \right)$$

$$\frac{V_0}{-200V_1} = \frac{2k}{\frac{1}{j\omega \cdot 1\mu F} + 2k} \rightarrow \frac{V_0}{-200V_1} \Big|_{\omega \rightarrow \infty} = 1$$

$$\frac{|V_0(j\omega)|}{-200|V_1(j\omega)|} = \frac{1}{\sqrt{2}}$$

3dB is when  $\frac{V_0}{V_1} = \frac{1}{\sqrt{2}}$

PS2 Q6

Miller:

$$k = \frac{V_o}{V_{\pi}} = \frac{-5k \parallel 1k \cdot 0.1 \cancel{\mu} \cdot V_{\pi}}{V_{\pi}}$$

siemens

$$= \frac{-5k}{1k+5k} \cdot 1k \cdot 100m\cancel{\mu}$$
$$= -0.833 \cdot 100$$
$$= -83.3$$

$$W_{HP1} = \frac{1}{50\Omega \parallel 50k\Omega \parallel 2.5k\Omega \cdot 88.3pF}$$

$$W_{HP2} = \frac{1}{833\Omega \cdot 1pF}$$

$$A_m = \frac{V_o}{V_i} = \frac{V_o}{V_{\pi}} \cdot \frac{V_{\pi}}{V_i}$$

$$= -83.3 \cdot \frac{50k \parallel 2.5k}{50k \parallel 2.5k + 50} \approx \boxed{-83.3 \frac{V}{V}}$$

$$W_{LP1} = \frac{1}{(50\Omega + 50k \parallel 2.5k) 2\mu F}$$

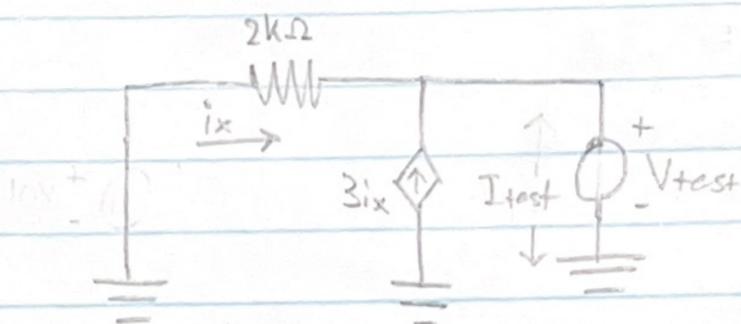
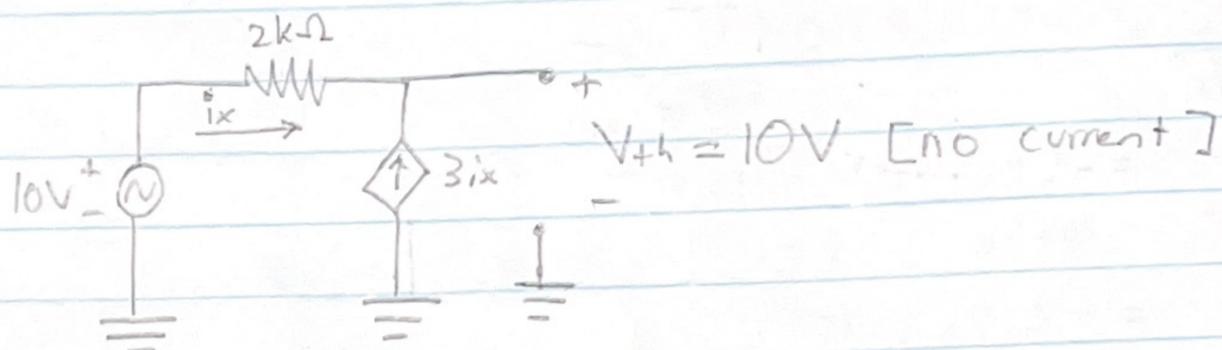
$$W_{LP2} = \frac{1}{6k \cdot 0.1\mu F}$$

$$T(s) = A_m \cdot \frac{s}{s+W_{LP1}} \cdot \frac{s}{s+W_{LP2}} \cdot \frac{W_{HP1}}{s+W_{HP1}} \cdot \frac{W_{HP2}}{s+W_{HP2}}$$

$$\boxed{W_{L3DB} = 1680/s}$$

$$W_{L3DB} = \sqrt{W_{LP1}^2 + W_{LP2}^2}$$

PS1 Q2



$$i_x = \frac{V_{test}}{2k} \quad I_{test} = 4i_x$$

$$R_{test} = \frac{V_{test}}{I_{test}} = \frac{i_x \cdot 2k}{4i_x} = 500\Omega = R_{th}$$

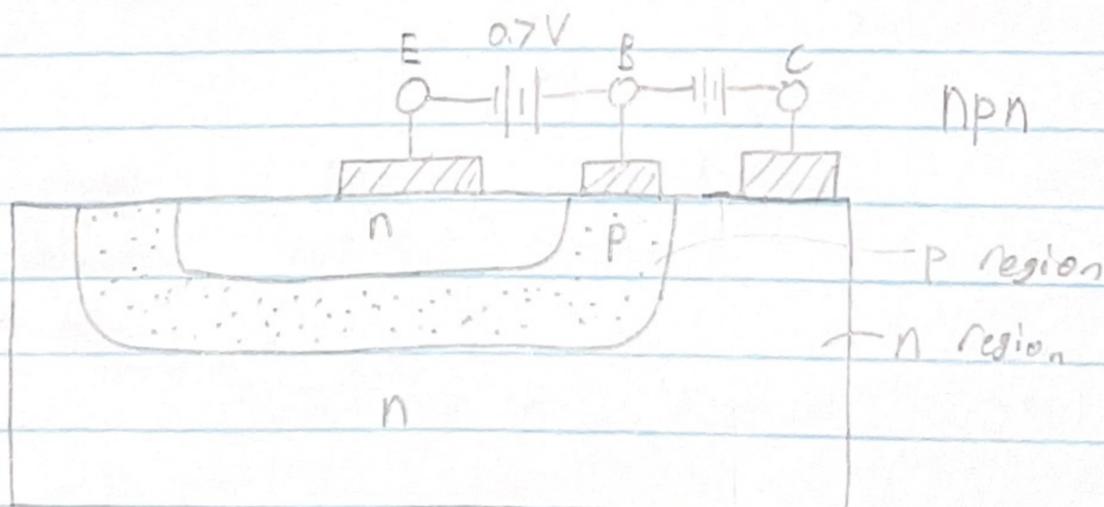
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Lecture 10

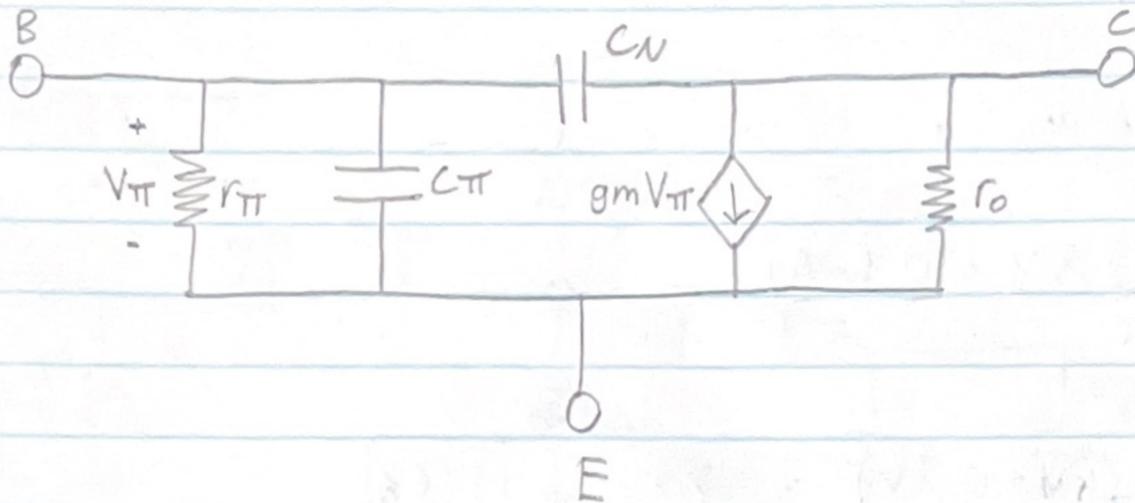
558 The BJT as an amplifier:

10/01/19  
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Lecture 11



## Hybrid- $\pi$ small signal Model:



Formulas:

$$i_c = \frac{I_c}{V_T} \cdot V_{be} = g_m V_{be}$$

$$r_{\pi} = \frac{V_{be}}{i_b}$$

**PS3 Q1**  $V_{CC} = 15V$   
 $I_C = 2mA$

$$R_C = \frac{V_{CC} - V_C}{I_C} = \frac{\frac{1}{3}V_{CC}}{I_C} = \frac{5V}{2mA} = \boxed{2.5k\Omega}$$

$$I_E \approx I_C = 2mA \quad R_E = \frac{4.3V}{2mA} = \boxed{2.15k\Omega}$$
$$V_E = V_B - 0.7V = 4.3V$$

$$R_{B1} = \frac{V_{CC} - V_B}{0.1(2mA)} = \frac{10V}{0.2mA} = \boxed{50k\Omega}$$

$$R_{B2} = \frac{V_C - V_B}{0.2mA - \frac{I_E}{100}} = \frac{5V}{0.18mA} = \boxed{27.8k\Omega}$$

# Lecture 12

10/03/19

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PS3 Q2

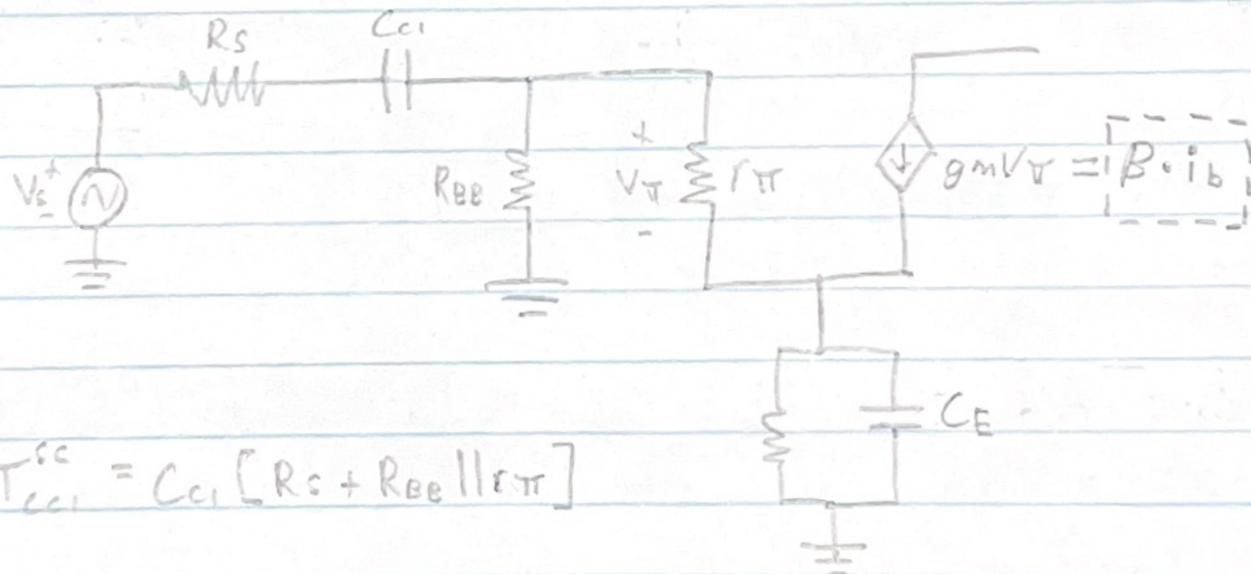
$$R_E = 8k = R_C$$

$$I_C = \frac{12V - \left(\frac{2}{3}\right)8V}{8k} = 0.5mA$$

$$R_{E1} = \frac{12V - (4V + 0.7V)}{0.5mA/10} = \frac{7.3V}{0.05mA} = 146k$$

$$R_{E2} = \frac{4.7V}{0.5mA/10 - 0.5mA/100} = \frac{4.7V}{0.045mA} = 104.4k$$

Low frequency Response Small signal:



$$T_{C_{c1}}^{sc} = C_{c1} [R_s + R_{ee} \parallel r_{\pi}]$$

$$T_{C_{c1}}^{oc} = C_{c1} [R_s + R_{ee} \parallel R_b]$$

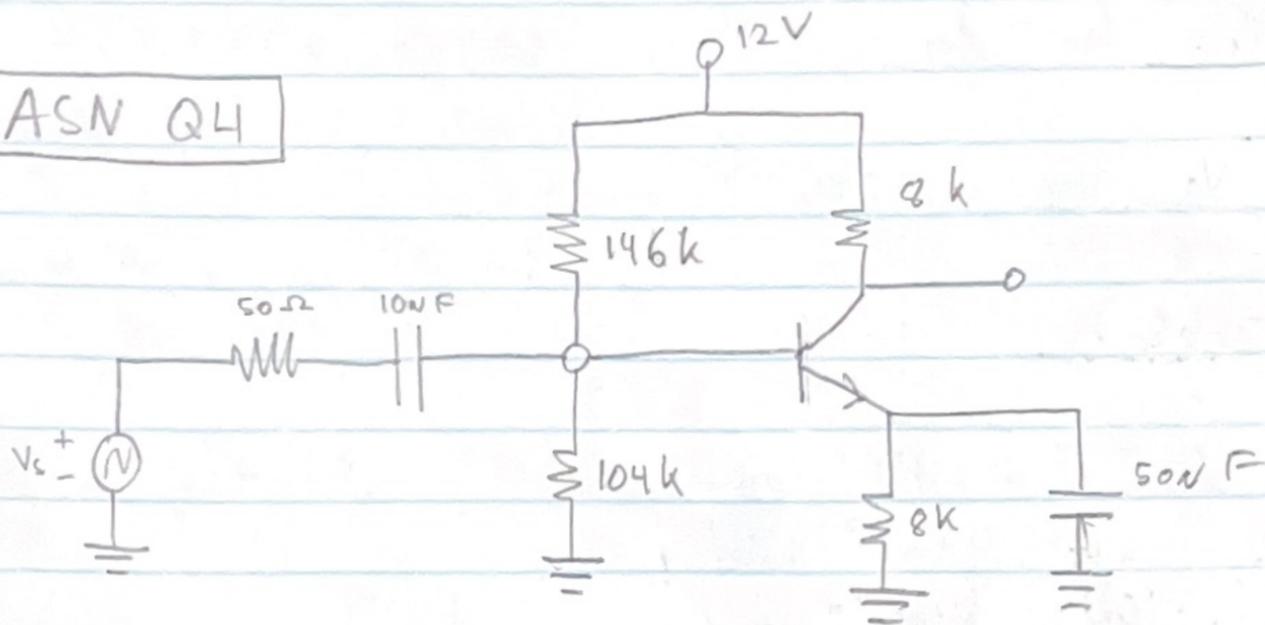
where:

$$R_b = r_{\pi} + (1 + \beta)R_e$$

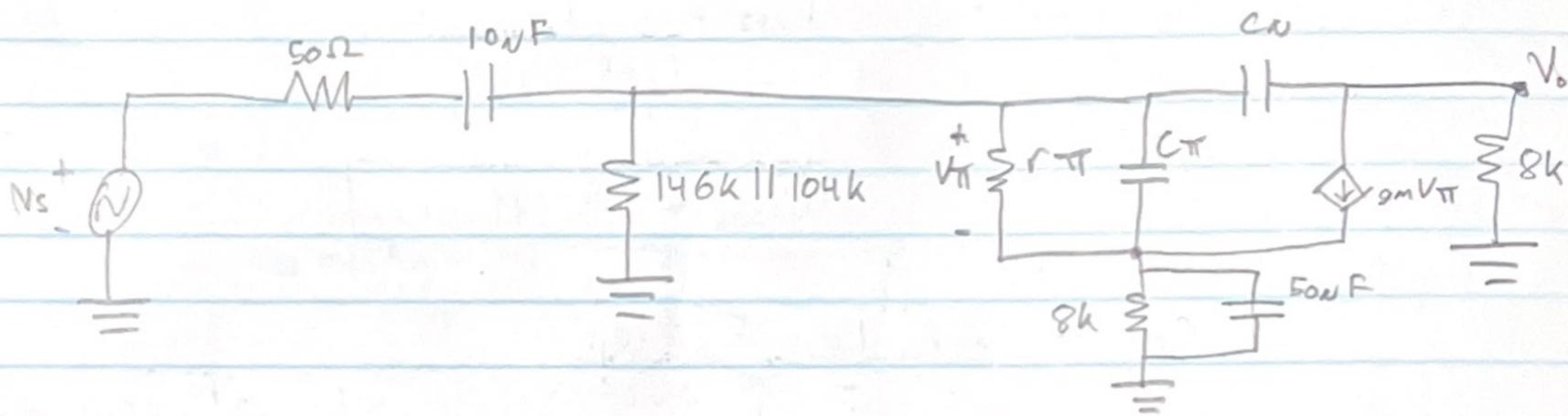
# Lecture 13

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ASN Q4



Small signal - Model:



Low FREQ model:

- Open  $C_{\pi}$  and  $C_M$

Midband FREQ model:

- ① open  $C_{\pi}$  and  $C_M$
- ② short  $10nF$  and  $50nF$

High FREQ model:

- short  $10nF$  and  $50nF$

$R_{BB}$

Solving for  $A_M$ :

\*note  $r_{\pi} = 5k$

\*note  $(5k || 60.7k) = 4.62k$

$$A_M = \frac{V_o}{V_{\pi}} \cdot \frac{V_{\pi}}{V_s} = -20mV \cdot 8k \cdot \frac{4.62k}{4.67k}$$

$$A_M = -158 \frac{V}{V}$$

Solving for High FREQ:

$$K = \frac{V_o}{V_{\pi}} = -160, \quad \omega_{HP1} = \frac{1}{(50\Omega || 4.62k\Omega)(C_{\pi} + C_M \cdot 161)}$$

$$\omega_{HP2} = \frac{1}{(2pF)(8k)}$$

$$\omega_{H3dB} = 43.4 M rad/s$$

Solving for Low FREQ:

Zero @ 50nF Capacitor:

$$8k + \frac{1}{sCE} \rightarrow \infty \quad [\text{For } gmV_{\pi} = 0]$$

# Lecture 14

10/15/19

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SS 11.5 Midband Analysis:

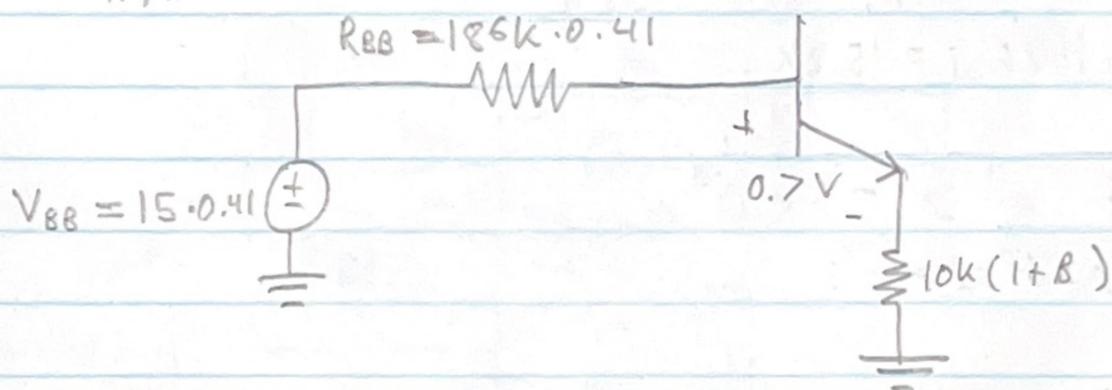
$$A_M = \frac{V_o}{V_s} = \frac{V_o}{V_{\pi}} \cdot \frac{V_{\pi}}{V_s}$$

$$\frac{V_o}{V_{\pi}} = -g_m R_c \parallel R_L, \quad \frac{V_{\pi}}{V_s} = \frac{-R_c \parallel \frac{r_{\pi}}{1+\beta}}{R_c \parallel \frac{r_{\pi}}{1+\beta} + R_s}$$

$$A_M =$$

PS4 Q2

$$\frac{127k}{186k + 127k} = 0.41$$



$$V_{BB} = I_B R_{BB} + 0.7V + I_B (10k)$$

$$I_B = \frac{15 \cdot 0.41 - 0.7}{186k \cdot 0.41 + 1.01M\Omega} = 5 \mu A$$

$$I_C = \beta I_B = 500 \mu A$$

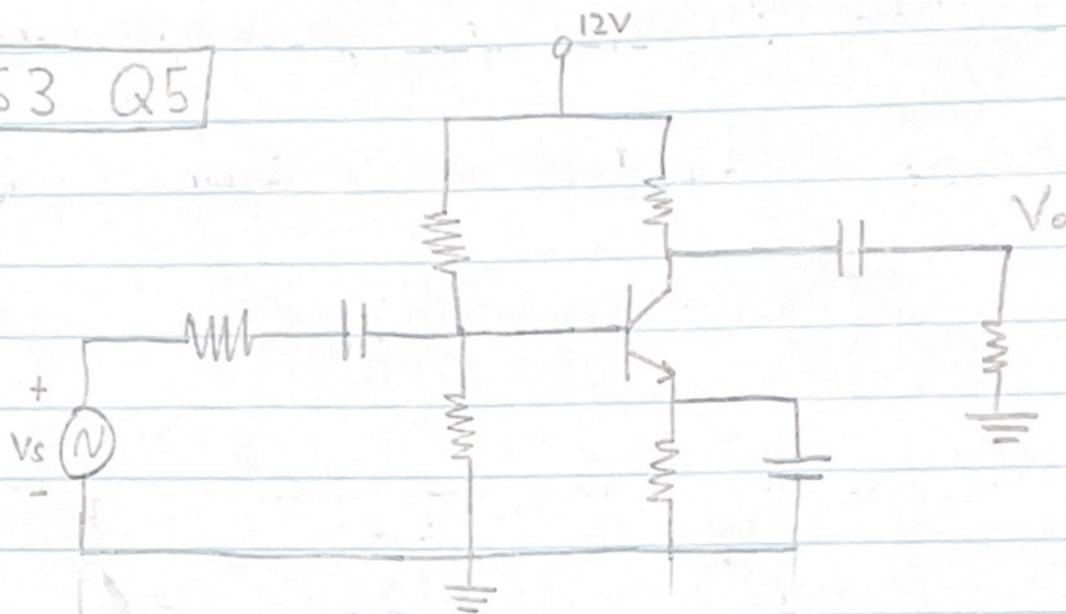
$$g_m = 20mS, \quad V_{\pi} = 5k$$

# Lecture 15

10/17/19  
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\* No  $\frac{1}{3}$  rule for already biased circuits  
ie: Q1, Q3

PS3 Q5



$$I_C = 2 \text{ mA}$$

$$\beta = 100$$

$$V_{BE} = 80 \text{ mV}$$

$$r_{\pi} = 1.25 \text{ k}$$

$$r_{BB} = 36.5 \parallel 26.1 = 15.2 \text{ k}$$

\* Use model from

SS 10.4

$$W_{LP3} = \frac{1}{4 \text{ k} \cdot 0.5 \text{ nF}} = 0.5 \times 10^3 / \text{sec}$$

$$T_{CE}^{sc} = 50 \text{ nF} \cdot 2 \text{ k} \parallel \left( \frac{r_{\pi} + r_{BB} \parallel 50}{1 + \beta} \right) \checkmark \text{ Higher FREQ dominant pole}$$

\*  $T_{CE}^{sc} < T_{CE1}^{sc}$

$$T_{CE1}^{sc} = 50 \text{ nF} \cdot (50 \Omega + r_{BB} \parallel r_{\pi})$$

$$W_{LP2} = \frac{1}{T_{CE1}^{sc}} = 1.666 \times 10^3 / \text{s}$$

# Lecture 16

10/21/19

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## Questions

- ①  $I_c$  vs  $V_{ce}$  with variable  $V_{BE}$ , sweep parameters for  $V_{be}$
- ② Transconductance  $g_m = \frac{I_c}{V_T}$  'or' from slope of  $I_c$  vs  $V_{be}$

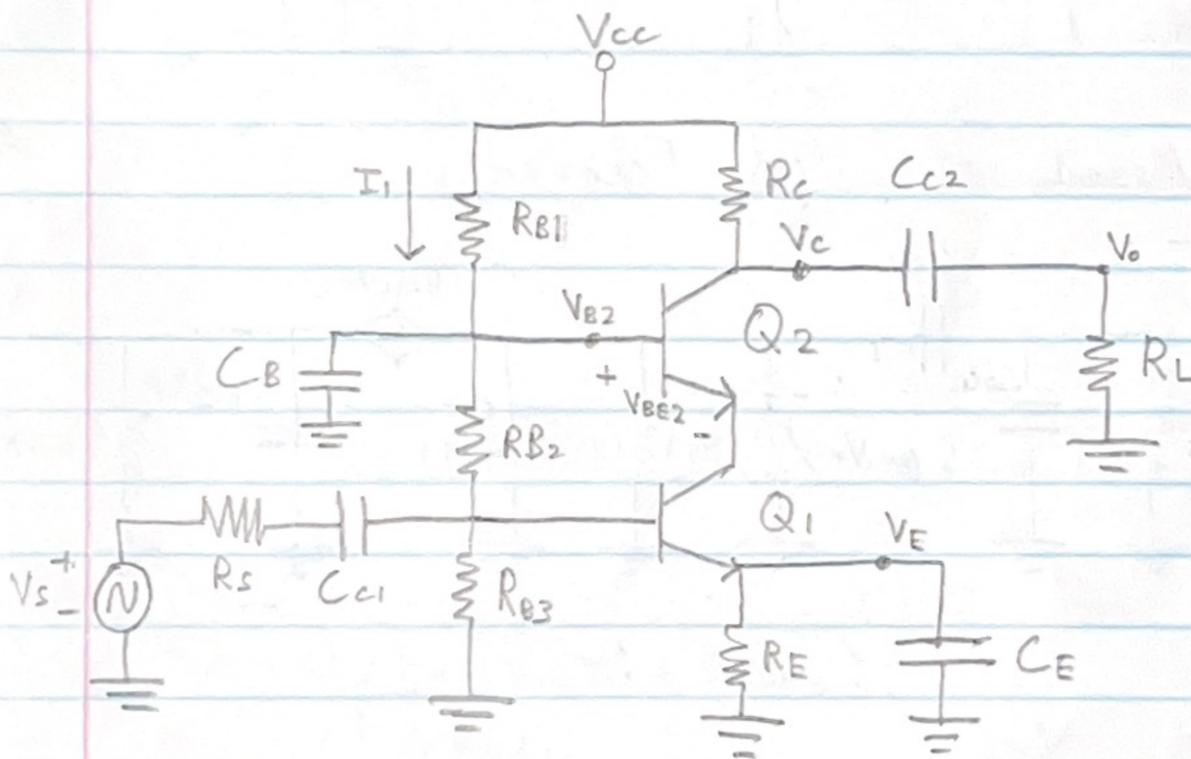
0.6 - 0.7

10/24/19

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# Lecture 17

## (CASCODE AMPLIFIER)



### 1/4 Rule Biasing

\*Note:  $V_{B1} = \frac{1}{4}V_{cc} + V_{BE1}$  (By biasing) = 0.7V

$$I_1 = 0.1 I_E$$

①  $V_{cc} - V_c = \frac{1}{4} V_{cc}$

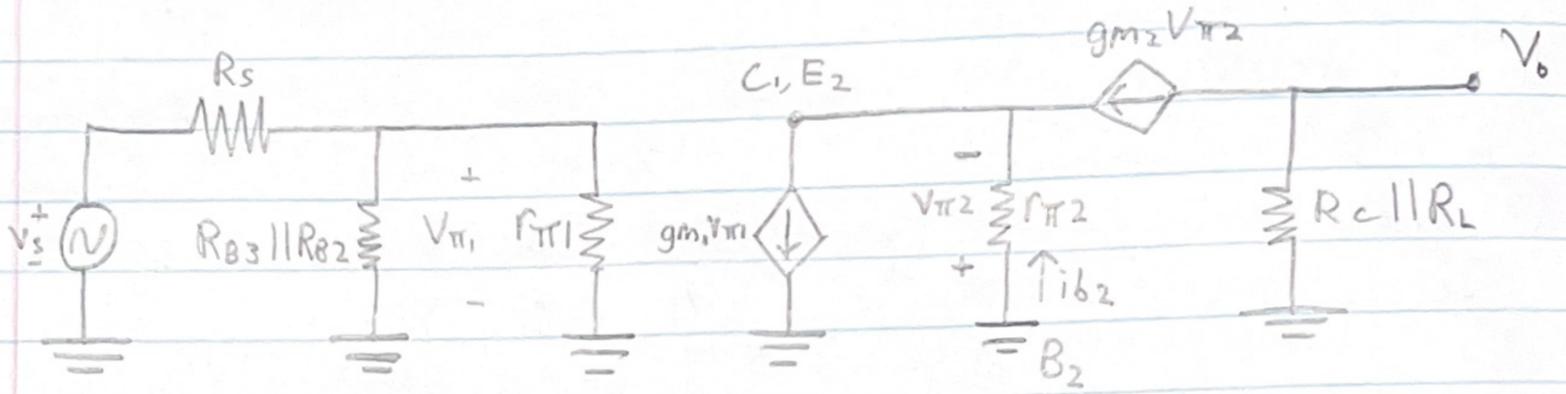
②  $V_E = \frac{1}{4} V_{cc}$

③  $V_{B2} = \frac{1}{2} V_{cc} + V_{BE2}$

$V_{BE2} \approx 0.7V$

$$r_{\pi} = \frac{\beta V_T}{I_C}$$

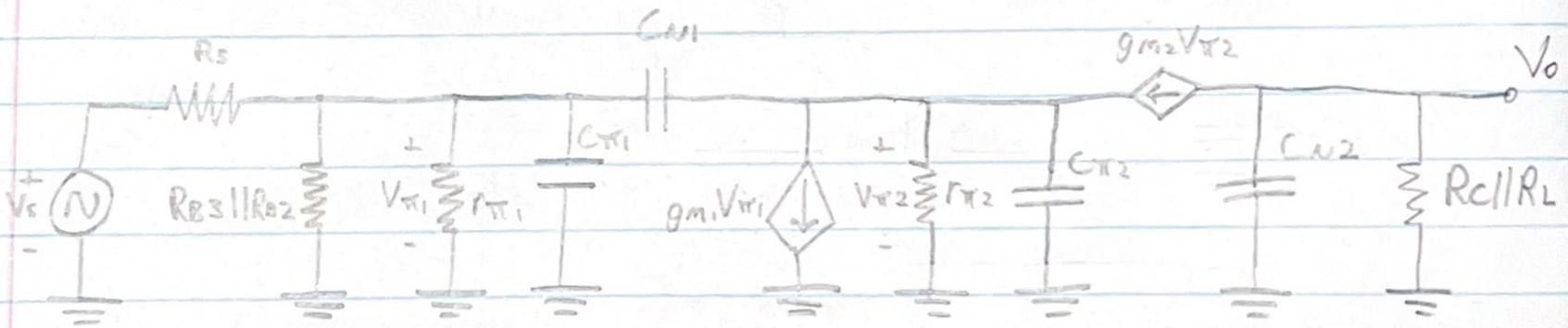
### Small Signal Model at MidBand:



$$g_{m1} V_{\pi 1} = \frac{V_{\pi 2}}{r_{\pi 2}} + g_{m2} V_{\pi 2}$$

$$\frac{\beta}{r_{\pi 1}} V_{\pi 1} = \left( \frac{1 + \beta_2}{r_{\pi 2}} \right) V_{\pi 2}$$

### Small Signal Model at High Frequency:



$$A_M = \frac{V_o}{V_{\pi 2}} \cdot \frac{V_{\pi 2}}{V_{\pi 1}} \cdot \frac{V_{\pi 1}}{V_s}$$

Calculated  
above

$$= -g_{m2} R_c || R_L \cdot 1 \cdot \frac{R_{B3} || R_{B2} || r_{\pi 1}}{R_{B3} || R_{B2} || r_{\pi 1} + R_s}$$

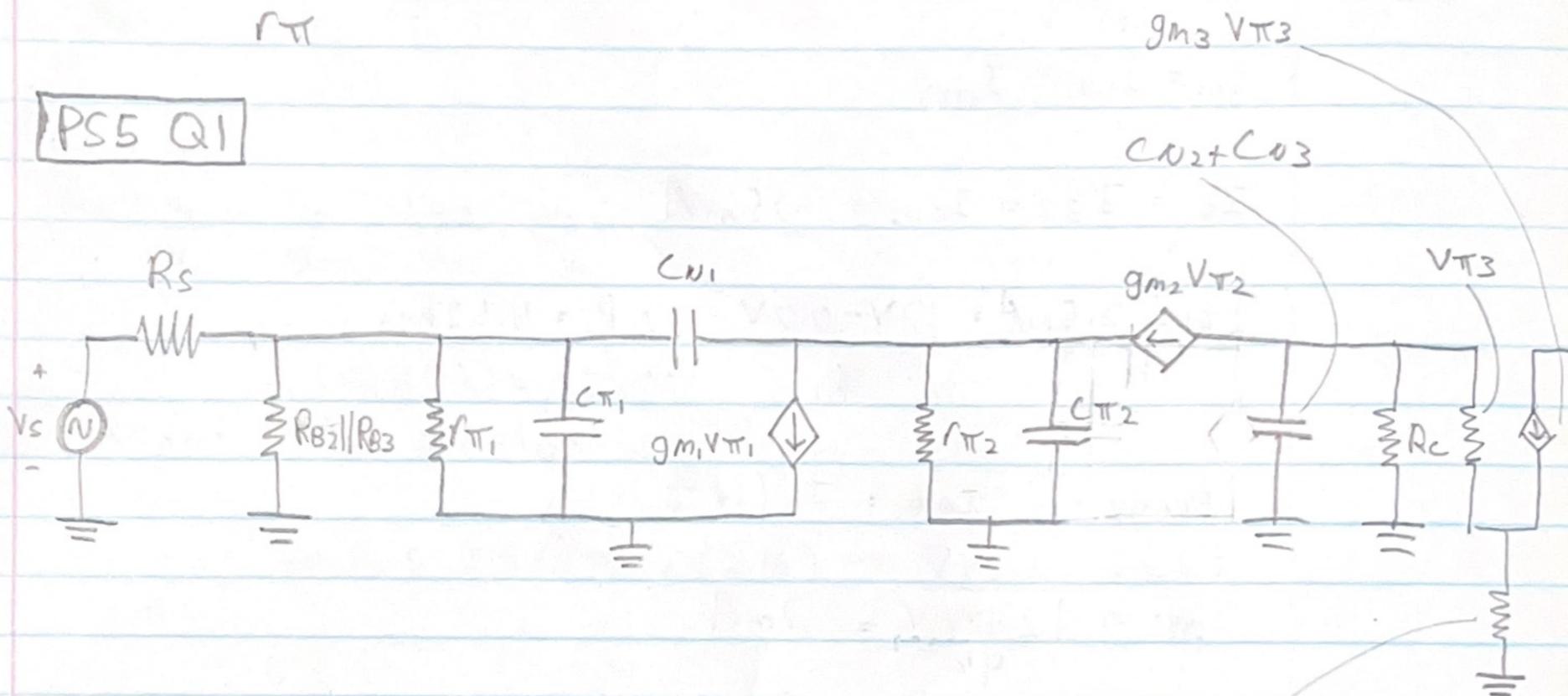
# Lecture 14

10/31/19  
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SS 14.1 Figure 1 → Figure 2 [small signal model]

$$g_{\pi} = \frac{1}{r_{\pi}}$$

PSS Q1



$$\omega_{HP1} = \frac{1}{R_s \parallel R_{B2} \parallel R_{B3} \parallel r_{\pi 1} (C_{\pi 1} + 2C_{n1})} \quad R_{E3} \parallel R_L$$

$$\omega_{HP2} = \frac{1}{\left( \frac{r_{\pi 2}}{1 + \beta_2} \right) (C_{\pi 2} + 2C_{n1})}$$

$$\omega_{HP3} = \frac{1}{[R_C \parallel (r_{\pi 3} + (1 + \beta_3) R_{E3} \parallel R_L)] (C_{n2} + C_{n3})} \quad \text{[Lowest HFP (dominant)]}$$

# Lecture 15

11/4/19  
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## PS6 Q1

$$a) I_{(8k)} = \frac{12V - 2V}{8k\Omega} = \frac{10V}{8k\Omega} = 1.25mA$$

$$I_{C1} = I_{C2} \approx I_{(8k)}$$

$$I_{E1} = I_{E2} = I_{C1,2} = 1.25mA$$

$$I_{R1} = 2.5mA = \frac{12V - 0.7V}{R_1} \quad \therefore R_1 = 4.52k\Omega$$

↓  
Because  $I_{REF} = I_0 \left(1 + \frac{2}{\beta}\right)$  ← negligible for large  $\beta$

$$I_{(4k)} = \frac{12V - 4V}{4k} = 2mA$$

$$I_{O2} = 4mA$$

$$R_2 = \frac{12V - 0.7V}{4mA} = 2.825k\Omega$$

$$b) I_{C1} = I_{C2} = 1.25mA$$

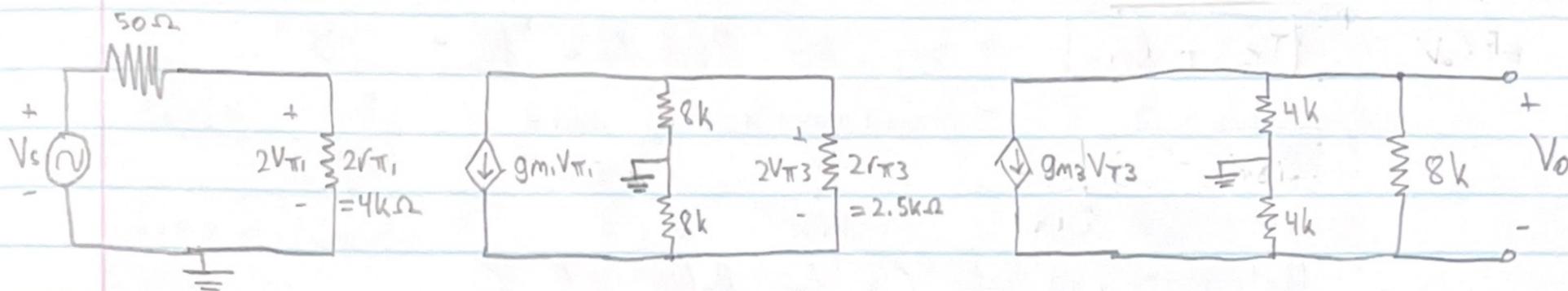
$$I_{C3} = I_{C4} = 4mA$$

$$g_{m1} = g_{m2} = 50mS$$

$$g_{m3} = g_{m4} = 80mS$$

$$r_{\pi 1} = r_{\pi 2} = \frac{100 \cdot 25mV}{1.25mA} = 2k\Omega$$

$$r_{\pi 3} = r_{\pi 4} = 1.25k\Omega$$



$$A_M = \frac{V_o}{V_s} = \frac{V_o}{V_{\pi 3}} \cdot \frac{V_{\pi 3}}{V_{\pi 1}} \cdot \frac{V_{\pi 1}}{V_s}$$

$$\frac{V_o}{V_{\pi 3}} = -g_{m3}(8k \parallel 8k) = -320 \frac{V}{V}$$

$$\frac{2V_{\pi 3}}{V_{\pi 1}} = -g_{m1}(2.5k \parallel 16k) = (5)(2)(2.16) \rightarrow \frac{V_{\pi 3}}{V_{\pi 1}} = -54.1 \frac{V}{V}$$

$$\frac{V_{\pi 1}}{V_s} = \frac{2V_{\pi 1}}{V_s} \cdot \frac{1}{2} = \frac{4k}{4.05k} \cdot \frac{1}{2} \approx \frac{1}{2} \frac{V}{V}$$

$$\therefore A_M = 8640 \frac{V}{V}$$

# Lecture 16

11/5/19  
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\*\* Test 03 → up to PS6 Q1 \*Not Q2

PS5 Q3

Match zero of  $C_E$  to Pole of  $C_{c1}$

$$1500 \text{ rad/s} = \frac{1}{C_E (4k \parallel \frac{r_{\pi 1} + 50 \parallel R_{B1} \parallel R_{B2}}{1 + \beta_1})}$$

$$1500 \approx \frac{1}{C_E (4k \parallel \frac{5k + 50}{201})}$$

$$\approx \frac{1}{C_E (25 \Omega)}$$

$$\therefore C_E = 26.6 \text{ nF}$$

$$\omega_{z_{C_E}} = \omega_{p_{C_{c1}}} = \frac{1}{26.6 \text{ nF} (4k \Omega)} = 9.375 \text{ rad/s}$$

$$9.375 \text{ rad/s} = \frac{1}{C_{c1} [50 + R_{B1} \parallel R_{B2} \parallel (r_{\pi 1} + (\beta_1 + 1) 4k)]}$$

$$R_{B1} = \frac{12V - 4V - 0.7V}{0.1 \text{ mA}} = 73k \Omega$$

$$R_{B2} = \frac{4 + 0.7V}{0.095 \text{ mA}} = 49.5k \Omega$$

$$C_{c1} = \frac{1}{9.375 (28.5k)}$$

$$\therefore C_{c1} = 3.8 \text{ nF}$$

PS5 Q2

$$I_{E1} = 2.5 \text{ mA}$$

$$I_{E2} = 10 \text{ mA}$$

From given voltages

$$\beta_1 = \beta_2 = 100$$

$$I = \frac{V}{R}$$

Not Specified:

$$\beta = 100$$

$$C_{\pi} = 10 \text{ pF}$$

$$C_u = 1 \text{ pF}$$

$$V_{BE} = 0.7 \text{ V}$$

$$g_{m1} = 100 \text{ mS}$$

$$r_{\pi 1} = 1 \text{ k}\Omega$$

$$g_{m2} = 400 \text{ mS}$$

$$r_{\pi 2} = 250 \Omega$$

$$\omega_{LP3} =$$

1

$$= 2300 \text{ rad/s}$$

$$\frac{22 \Omega + 930 \Omega \parallel \frac{250 \Omega + 2 \text{ k}\Omega}{\beta + 1}}{C_{\pi}}$$

11/7/19  
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## Lecture 17

PS5 Q2 (cont'd)

$$\omega_{HP1} = \frac{1}{47.5 \Omega \cdot 121 \text{ pF}} = 1.74 \times 10^8 \text{ rad/s}$$

$$\omega_{HP2} = \frac{1}{1.1 \text{ k}\Omega \cdot 2 \text{ pF}} = 4.55 \times 10^8 \text{ rad/s} \quad A_M = -94 \frac{\text{V}}{\text{V}}$$

\*\*  $C_{\pi 2}$  disappears by Pole-Zero Cancellation

\*\* Test 03  $\rightarrow$  Up to SS. 14

# Lecture 18

11/19/19  
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## PS7 Q4

$$V_{\pi 1} = 64.6 \text{ k}$$

$$V_{\pi 2} = 5.81 \text{ k}$$

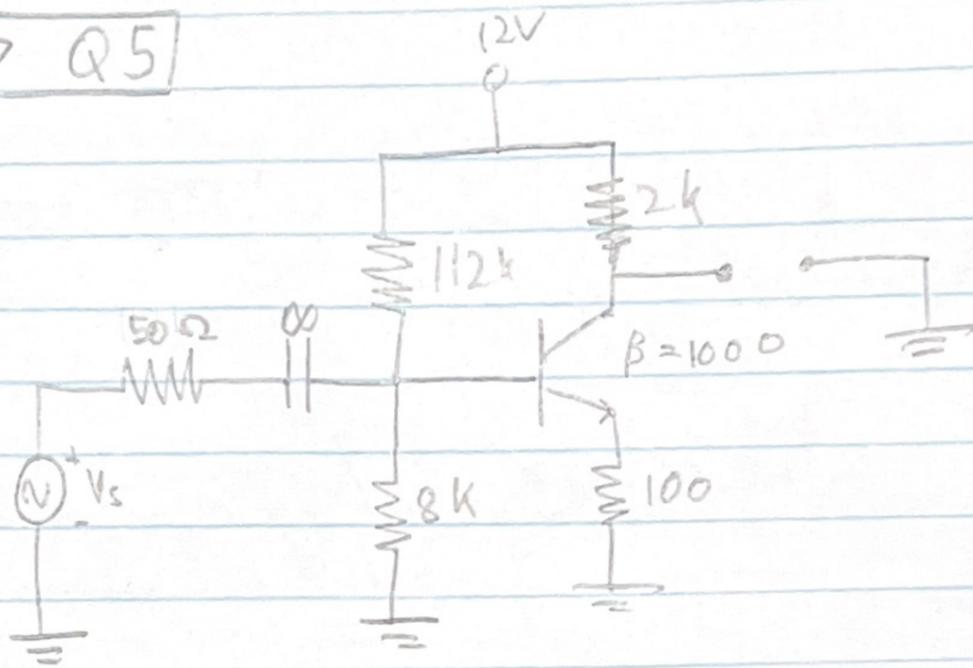
$$V_{\pi 3} = 12.9 \text{ k}$$

$$g_{m1} = 1.55 \text{ mS}$$

$$g_{m2} = 17.2 \text{ mS}$$

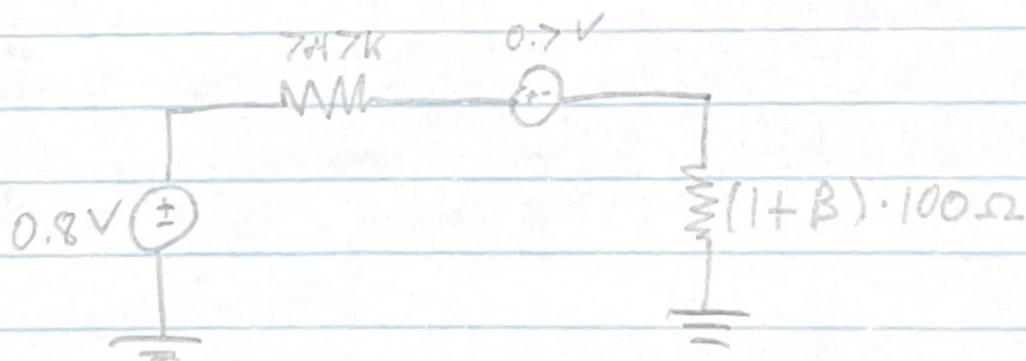
$$g_{m3} = 7.76 \text{ mS}$$

## PS7 Q5



$$V_{BB} = \frac{12\text{V} \cdot 8\text{k}}{112\text{k} + 8\text{k}} = 0.8\text{V}$$

$$R_{BB} = \frac{112\text{k} \cdot 8\text{k}}{120\text{k}} = 7.47\text{k}\Omega$$



$$I_B = \frac{0.8\text{V} - 0.7\text{V}}{7.47\text{k} + (1+\beta)(100)} = 0.93\text{ nA}$$

$$I_C = 0.93\text{ mA} \quad r_{\pi} = 26.9\text{ k}\Omega \quad g_m = 37.2\text{ mS}$$